

Sombor

Gutman

P_n

F_m

W

Sombor

Sombor

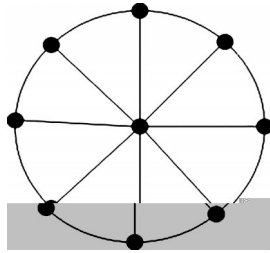
$$\begin{array}{l}
 1^{14} \\
 (u_1, v_1)
 \end{array}
 \begin{array}{l}
 G \quad H \\
 u_1 \hat{a} u_2 \quad v_1 \hat{a} v_2 \quad E(H) \quad v_1 = v_2 \quad u_1 u_2 \quad E(G) \quad 1
 \end{array}
 \begin{array}{l}
 V(G \quad H) = V(G) \times V(H) \\
 V(G \times H) = V(G) \times V(H)
 \end{array}
 \begin{array}{l}
 (u_1, v_1)
 \end{array}$$

2¹⁵

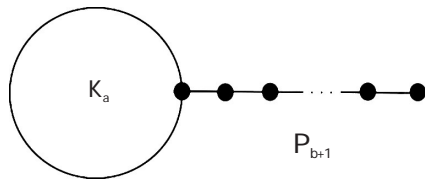
G H

$$V(G \times H) = V(G) \times V(H)$$

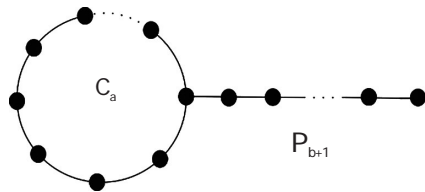
7	$N_{a,b}$	$b + 1$	P_{b+1}	a	C_a	6	
8		a	C_a	b	C_b	$b + 1$	$P_{b+1}(b - 1)$
C_b	P_{b+1}	$D_{a,b,c}$	7				C_a



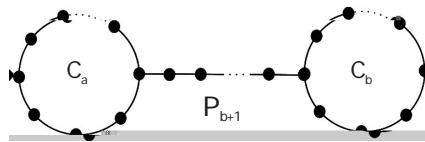
W_q



$N_{a,b}$



$L_{a,b}$



$D_{a,b,c}$

1

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1 $G = P_n W_m$ Sombor

$$SO(G) = (11mn - 9n - 20m + 14)\sqrt{2} + 2\sqrt{2m^2 + 2m + 1}$$

$$+(n - 2)(m - 1)\sqrt{m^2 + 2m + 26} + 2(m - 1)\sqrt{41} + 2(m - 1)\sqrt{m^2 + 16}$$

$v(G) = mn$ $e(G) = 3mn - m - 2n$ G $G = 4$ $G = m + 1$ $G = 2$

m m $(n - 2)(m - 1)$

$$= 2\sqrt{(m+1)^2 + m^2} + (n-2)(m-1)\sqrt{(m+1)^2 + 5^2} + (2n-5)(m-1)\sqrt{5^2 + 5^2}$$
$$+ 2(m-1)\sqrt{4^2 + 5^2} + 2(m-1)\sqrt{4^2 + 4^2} + 2(m-1)\sqrt{4^2 + m^2} + (n-3)\sqrt{(m+1)^2 + (\quad)}$$

$$SO(G) = \frac{1}{2}n(n^2a + n^2b + n^2c - n^2 + 2na + 2nb + 2nc - 10n + a + b + c - 13)\sqrt{2} + 6n\sqrt{2n^2 + 6n + 5}$$

$$v(G) = n(a + b + c - 1) \quad e(G) = \frac{1}{2}n(na + nb + nc - n + a + b + c + 1) \quad G \quad g = n + 1$$

$$g = n + 2 \quad n(n - 1) \quad 6n$$

$$\frac{1}{2}n(na + a + nb + b + nc + c - 3n - 9) \quad G \quad \text{Sombor}$$

$$SO(G) = \frac{1}{2}n(n^2a + n^2b + n^2c - n^2 + 2na + 2nb + 2nc - 10n + a + b + c - 13)\sqrt{2} + 6n\sqrt{2n^2 + 6n + 5}$$

$$8 \quad G = N_{ab} \quad K_n \quad \text{Sombor}$$

$$SO(G) = \frac{1}{2}n(an^2 + bn^2 + 2an + 2bn + a + b - 8n - 8)\sqrt{2} + 3n\sqrt{2n^2 + 6n + 5} + n\sqrt{2n^2 + 2n + 1}$$

$$v(G) = n(a + b) \quad e(G) = \frac{1}{2}n(na + nb + a + b) \quad G \quad g = n \quad g = n + 2$$

$$\frac{1}{2}n(n - 1) \quad 3n \quad (g + 1) \quad \frac{1}{2}n(an + bn - 2n + a + b - 6)$$

$$(g + 1) \quad n \quad (g + 1) \quad \frac{1}{2}n(n - 1) \quad G \quad \text{Sombor}$$

$$SO(G) = \frac{1}{2}n(an^2 + bn^2 + 2an + 2bn + a + b - 8n - 8)\sqrt{2} + 3n\sqrt{2n^2 + 6n + 5} + n\sqrt{2n^2 + 2n + 1}$$

3 Sombor

Sombor

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$$9 \quad G \quad n \quad k- \quad H$$

$$SO(G \times H) = nk^2SO(H)$$

$$V(G) = \{u_1, u_2, \dots, u_n\} \quad V(H) = \{v_1, v_2, \dots, v_m\} \quad E(G) = \{u_i u_j | 1 \leq i, j \leq n\} \quad E(H) = \{v_s v_t | 1 \leq s, t \leq m\}$$

$$V(G \times H) = \{u_i v_s | 1 \leq i \leq n, 1 \leq s \leq m\} \quad E(G \times H) = \{(u_i v_s)(u_j v_t) | 1 \leq i, j \leq n, 1 \leq s, t \leq m\} \quad d_G(u_i) = k$$

$$d_{G \times H}(u_i v_s) = d_G(u_i) d_H(v_s) = kd_H(v_s). \quad e_1 = (u_i v_s)(u_j v_t) \quad E(G \times H) \quad e_2 = (u_i v_s)(u_i v_t) \quad E(G \times H)$$

$$e(G \times H) = 2e(G)e(H) \quad d_{G \times H}(u_i v_s) = d_{G \times H}(u_j v_s) \quad d_{G \times H}(u_i v_t) = d_{G \times H}(u_j v_t)$$

$$SO(G \times H) = \sum_{(u_i v_s)(u_j v_t) \in E(G \times H)} \sqrt{d_{G \times H}^2(u_i v_s) + d_{G \times H}^2(u_j v_t)} = 2k \frac{nk}{2} \sum_{v_s v_t \in E(H)} \sqrt{d_H^2(v_s) + d_H^2(v_t)} = nk^2SO(H)$$

4 Sombor

Sombor

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$$10 \quad 1 \quad SO(K_n \times P_m) = 2n\sqrt{2n^2 + 2n + 1} + \left(\frac{1}{2}mn^3 + mn^2 + \frac{1}{2}mn - 4n^2 - 2n\right)\sqrt{2}$$

$$2 \quad SO(K_n \times C_m) = \frac{1}{2}nm(m + 1)(n + 1)\sqrt{2}$$

$$3 \quad SO(K_n \times P_m) = (2n^3 - 4n^2 + 2n)\sqrt{5} + (2n^3m - 4n^2m - 6n^3 + 12n^2 + 2nm - 6n)\sqrt{2} \quad (m > 2)$$

$$4 \quad SO(K_n \times C_m) = nm(m - 2)(n - 1)\sqrt{2}$$

$$5 \quad SO(K_n \times P_m) = 2n^2\sqrt{13n^2 - 10n + 2} + \left(\frac{9}{2}n^3m - 3n^2m - 10n^3 + 4n^2 + \frac{1}{2}nm\right)\sqrt{2} \quad (m > 2)$$

$$6 \text{ SO}(K_n \ C_m) = \frac{1}{2} nm(3n - 1)^2 \sqrt{2}$$

$$7 \text{ SO}(P_n \times P_m) = 4\sqrt{17} + (8m + 8n - 48)\sqrt{5} + (8mn - 24m - 24n + 80)\sqrt{2} \quad (m, n > 2)$$

$$8 \text{ SO}(C_n \times C_m) = 8mn\sqrt{2}$$

$$9 \text{ SO}(C_n \times P_m) = 8n\sqrt{5} + (8nm - 12n)\sqrt{2} \quad (m > 2)$$

$$10 \text{ SO}(P_n \ P_m) = (32mn - 78m - 78n + 200)\sqrt{2} + 8\sqrt{34} + 4\sqrt{53} + (6m + 6n - 32)\sqrt{89} \quad (m, n > 2)$$

$$11 \text{ SO}(C_n \ C_m) = 32mn\sqrt{2}$$

$$12 \text{ SO}(C_n \ P_m) = (32mn - 78n)\sqrt{2} + 6n\sqrt{89}.$$

$$\begin{array}{l} 1 \quad v(K_n \ P_m) = mn \quad e(K_n \ P_m) = \frac{1}{2} mn^2 + \frac{1}{2} mn - n \quad K_n \ P_m \quad K_n \ P_m = n \\ \quad K_n \ P_m = n + 1 \quad n^2 - n \quad 2n \\ \left(\frac{1}{2} mn^2 + \frac{1}{2} mn - n^2 - 2n \right) \quad K_n \ P_m \quad \text{Sombor} \end{array}$$

$$2 \quad G \quad n \quad k - \quad G \quad \text{Sombor} \quad \text{SO}(G) = \frac{nk^2}{\sqrt{2}} \quad K_n \ C_m$$

$$mm \quad (n + 1) - \quad \text{SO}(K_n \ C_m) = \frac{1}{2} nm(m + 1)(n + 1)\sqrt{2}$$

$$3 \quad K_n \times P_m \quad 10 \quad K_n \ n \quad n - 1 -$$

$$\text{SO}(K_n \times P_m) = nk^2 \text{SO}(H) = n(n - 1)^2 [2\sqrt{5} + 2(m - 3)\sqrt{2}]$$

$$= (2n^3 - 4n^2 + 2n)\sqrt{5} + (2n^3m - 4n^2m - 6n^3 + 12n^2 + 2nm - 6n)\sqrt{2} \quad (m > 2)$$

$$4 \quad K_n \times C_m \quad mn \quad (2n - 2) - \quad \text{SO}(K_n \times C_m) = nm(m - 2)(n - 1)\sqrt{2}$$

$$5 \quad v(K_n \ P_m) = mn \quad e(K_n \ P_m) = \frac{3}{2} mn^2 - n^2 - \frac{1}{2} mn \quad K_n \ P_m \quad K_n \ P_m = 2n - 1$$

$$K_n \ P_m = 3n - 1 \quad n^2 - n \quad 2n^2 \quad \left(\frac{3}{2} mn^2 - 4n^2 - \frac{1}{2} mn + n \right)$$

$K_n \ P_m \quad \text{Sombor}$

$$6 \quad K_n \ C_m \quad mn \quad (3n - 1) -$$

$$\text{SO}(K_n \ C_m) = \frac{1}{2} nm(3n - 1)^2 \sqrt{2}$$

$$7 \quad v(P_n \times P_m) = mn \quad e(P_n \times P_m) = 2(m - 1)(n - 1) \quad P_n \times P_m \quad P_n \times P_m = 1$$

$$P_n \times P_m = 4 \quad 4 \quad 4 \quad 2 \quad (4m + 4n - 24) \quad 2$$

$$(2mn - 6m - 6n + 18)$$

$P_n \times P_m \quad \text{Sombor}$

$$8 \quad C_n \times C_m \quad 10 \quad C_n \ 2 - \quad \text{SO}(C_n \times C_m) = nk^2 \text{SO}(C_m) =$$

$$n^2 2m\sqrt{2} = 8mn\sqrt{2}$$

$$9 \quad C_n \times P_m \quad 10 \quad C_n \ 2 - \quad \text{SO}(C_n \times P_m) = nk^2 \text{SO}(P_m) =$$

$$n^2 [2\sqrt{5} + 2(m - 3)\sqrt{2}] = 8n\sqrt{5} + (8nm - 12n)\sqrt{2}$$

$$10 \quad v(P_n \ P_m) = mn \quad e(P_n \ P_m) = 4mn - 3m - 3n + 2 \quad P_n \ P_m \quad P_n \ P_m = 3 \quad P_n \ P_m = 8$$

$$8 \quad 5 \quad 4 \quad (2m + 2n - 8) \quad 5$$

$$(6m + 6n - 32) \quad 5 \quad (4mn - 11m - 11n + 30)$$

$P_n \ P_m \quad \text{Sombor}$

$$11 \quad C_n \ C_m \quad mn \ 8 - \quad \text{SO}(C_n \ C_m) = \frac{mn8^2}{\sqrt{2}} = 32mn\sqrt{2}$$

$$12 \quad v(C_n, P_m) = mn \quad e(C_n, P_m) = 4mn - 3n \quad C_n, P_m \quad C_n, P_m = 5 \quad C_n, P_m = 8$$

$2n$
 C_n, P_m Sombor
 11 G

$$G = G_1, G_2, G_3, \dots, G_n$$

$$SO(G) > \sum_{i=1}^n SO(G_i)$$

$$E(G_i) \quad E(G) = E(G_1) + E(G_2) + E(G_3) + \dots + E(G_n) \quad G_i(1 \leq i \leq n) \quad v \quad V(G_i)$$

$$v \quad V(G) \quad d_G(v) \quad d_G(v) \quad e = uv \quad E(G_i) \quad e \quad E(G) \quad G_i \quad d_G(u) \quad G$$

$$SO(G) > SO(G_i) \quad d_G(u) \quad d_G(u) > d_G(u) \quad \sqrt{d_G^2(v) + d_G^2(u)} > \sqrt{d_{G_i}^2(v) + d_{G_i}^2(u)} \quad E(G_i) \quad E(G)$$

1 $G \quad H$

$$SO(G \times H) > SO(G \times H) + SO(G \times H)$$

$$G \times H = (G \times H) \quad (G \times H) \quad E(G \times H) = E(\quad)$$

~~$G \times H$~~

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Sombor Index of Several Kinds of Product Graphs

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Sombor index is a new topological index based on vertex degree introduced by Gutman in Chemical Graph Theory. In this paper Sombor indices of cartesian products of path P_n with fan graph F_m and wheel graph W_m wheel graph W_n with fan graph F_m and wheel graph W_m fan graph F_n with fan graph F_m and lollipop graph $N_{a,b}$ barbell graph $D_{a,b,c}$ and kite graph $L_{a,b}$ with complete graph K_n are discussed Sombor indices of Direct products Cartesian products and Strong products of complete graph path and cycle are also studied and the exact index values and some relations of sombor indices about product graph are obtained.

Sombor index Cartesian product Direct product Strong product

9

Bayes Estimation of the Shape Parameter of Pareto Distribution under the Gradually Increasing of Type Truncation

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Based on gradually increasing type truncated samples. Firstly obtain the maximum likelihood estimation of the Pareto distribution shape parameter considering the two loss functions and the two prior distributions of shape parameters four Bayes estimation of the distribution shape parameter is concluded. It is found from the numerical simulation results that the mean square error of the four Bayes estimates is less than the maximum likelihood estimate. Among them when the loss function is a quadratic loss function and the prior distribution of the shape parameter is a conjugate prior distribution and the estimation effect is more ideal and the example analysis is consistent with the numerical simulation results. Secondly under the quadratic loss function truncation of the shape parameters of the Pareto distribution are given.

Gradually increasing of type truncation Pareto distribution Quadratic loss Q- symmetry entropy loss Bayes estimates